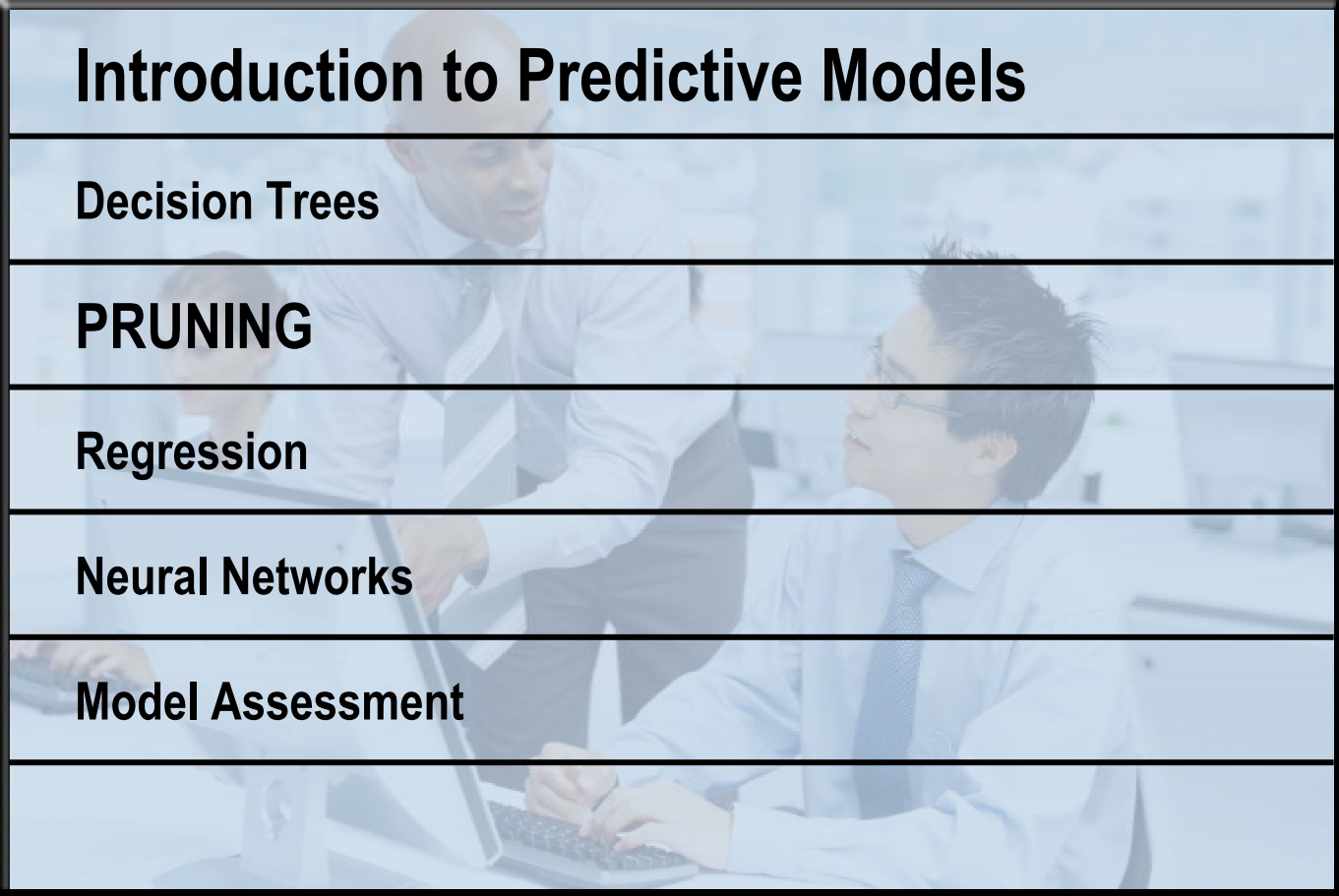


Agenda



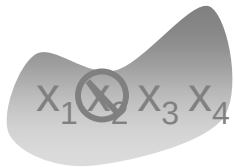
Introduction to Predictive Models
Decision Trees
PRUNING
Regression
Neural Networks
Model Assessment

Model Essentials – Decision Trees



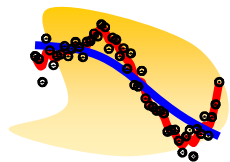
Predict new cases

Prediction rules



Select useful inputs

Split search



Optimize complexity

Pruning

Binary Targets

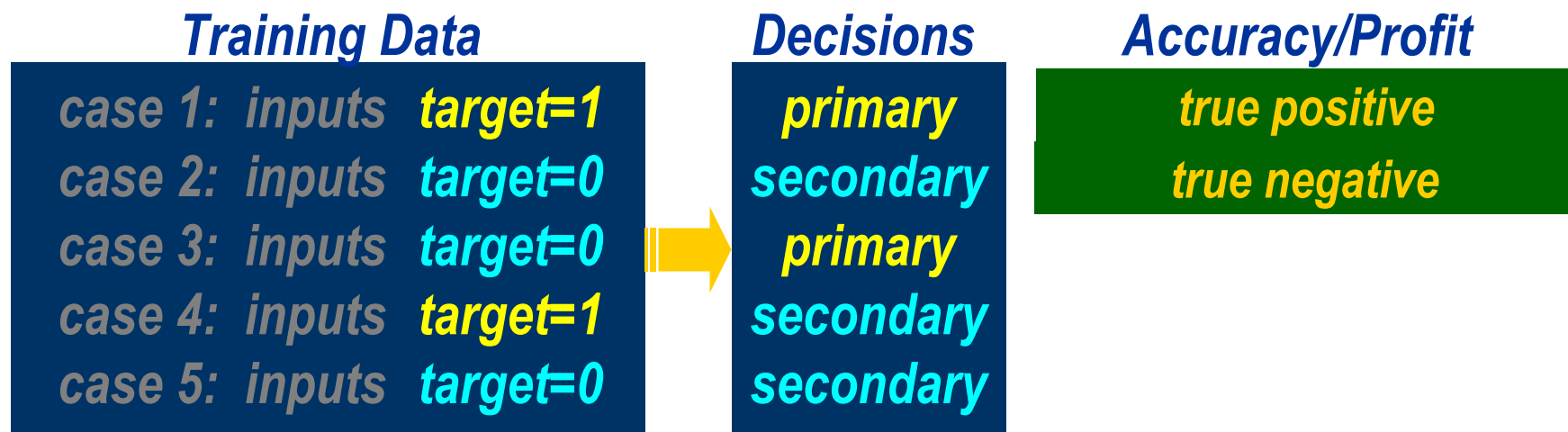
Training Data

<i>case 1: inputs</i>	<i>target=1</i>
<i>case 2: inputs</i>	<i>target=0</i>
<i>case 3: inputs</i>	<i>target=0</i>
<i>case 4: inputs</i>	<i>target=1</i>
<i>case 5: inputs</i>	<i>target=0</i>

primary outcome

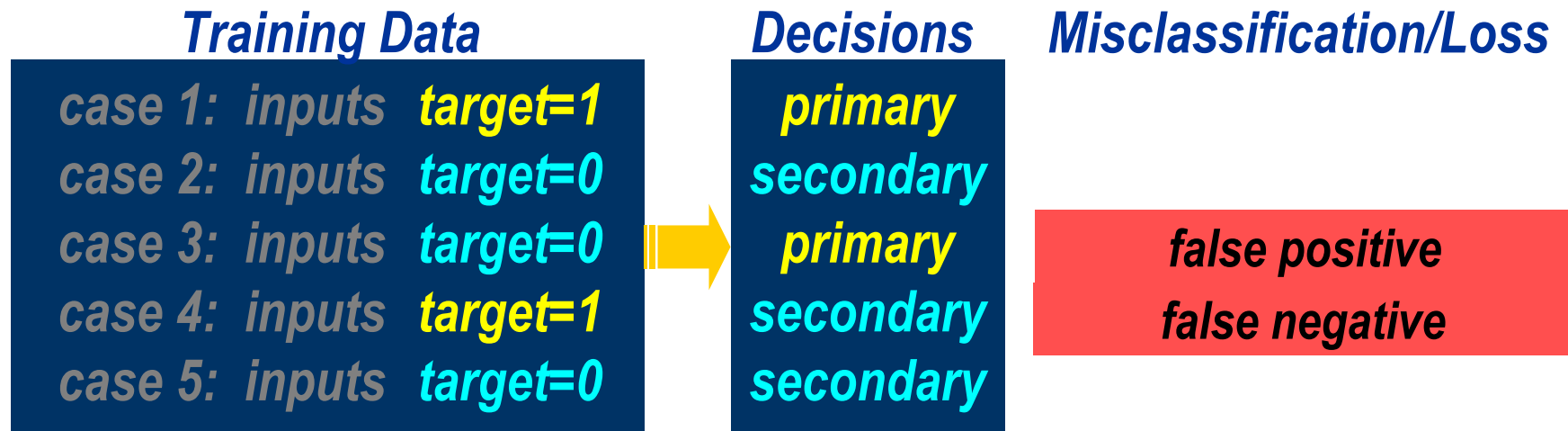
secondary outcome

Decision Assessment



Focus on correct decisions

Decision Assessment (for Pessimists)



Focus on incorrect decisions

Ranking Assessment

Training Data

case 1: inputs **target=1**
case 2: inputs **target=0**
case 3: inputs **target=0**
case 4: inputs **target=1**
case 5: inputs **target=0**



Rankings

720
520
620
580
470

Concordance

rank(target=1) >
rank(target=0)

Focus on correct ordering

Ranking Assessment (for Pessimists)

<i>Training Data</i>	<i>Rankings</i>	<i>Discordance</i>
case 1: inputs target=1	720	$\text{rank}(\text{target}=1) < \text{rank}(\text{target}=0)$
case 2: inputs target=0	520	
case 3: inputs target=0	620	
case 4: inputs target=1	580	
case 5: inputs target=0	470	

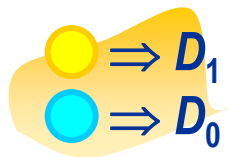
Focus on incorrect ordering

Estimate Assessment (only Pessimistic!)

Training Data	Estimates	Squared Error
case 1: inputs target=1	0.65	$(\text{target-estimate})^2$
case 2: inputs target=0	0.33	
case 3: inputs target=0	0.54	
case 4: inputs target=1	0.47	
case 5: inputs target=0	0.28	

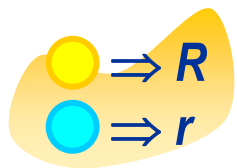
Focus on incorrect estimation

Predictive Modeling Assessments



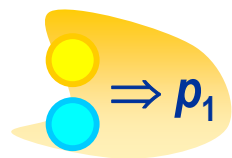
Decisions

**Accuracy
Misclassification**



Rankings

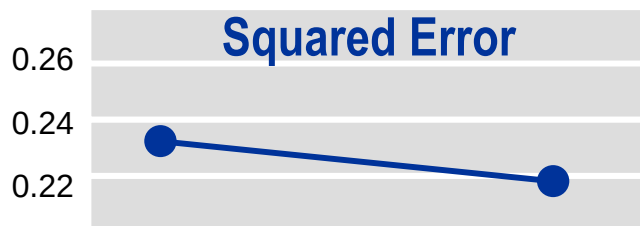
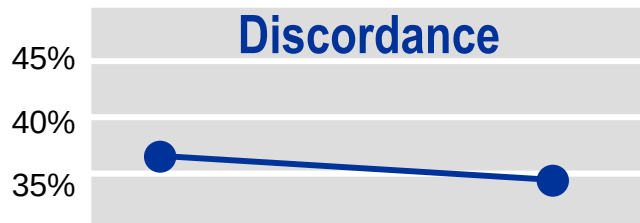
**Concordance
Discordance**



Estimates

Squared Error

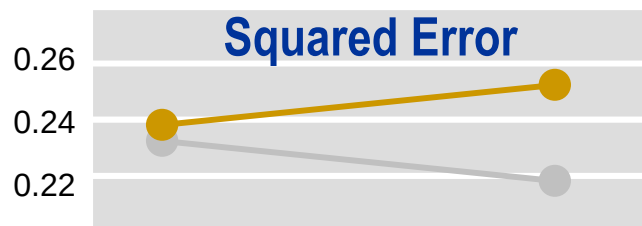
Optimistic Assessment, Pessimistic Stats



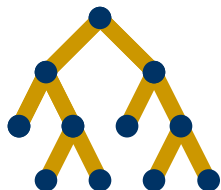
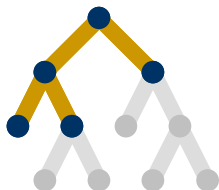
Increasing leaf count *improves* assessment measures on training data.



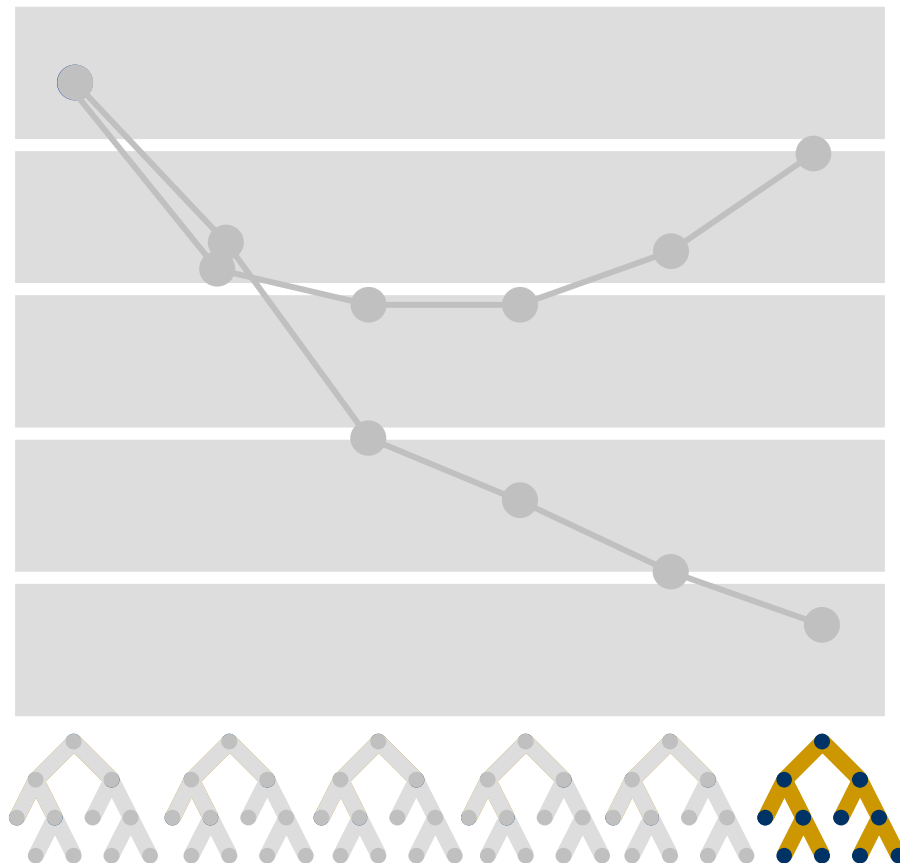
Unbiased Assessment



Increasing leaf count *might* worsen assessment measures on validation data.



Pruning Strategy

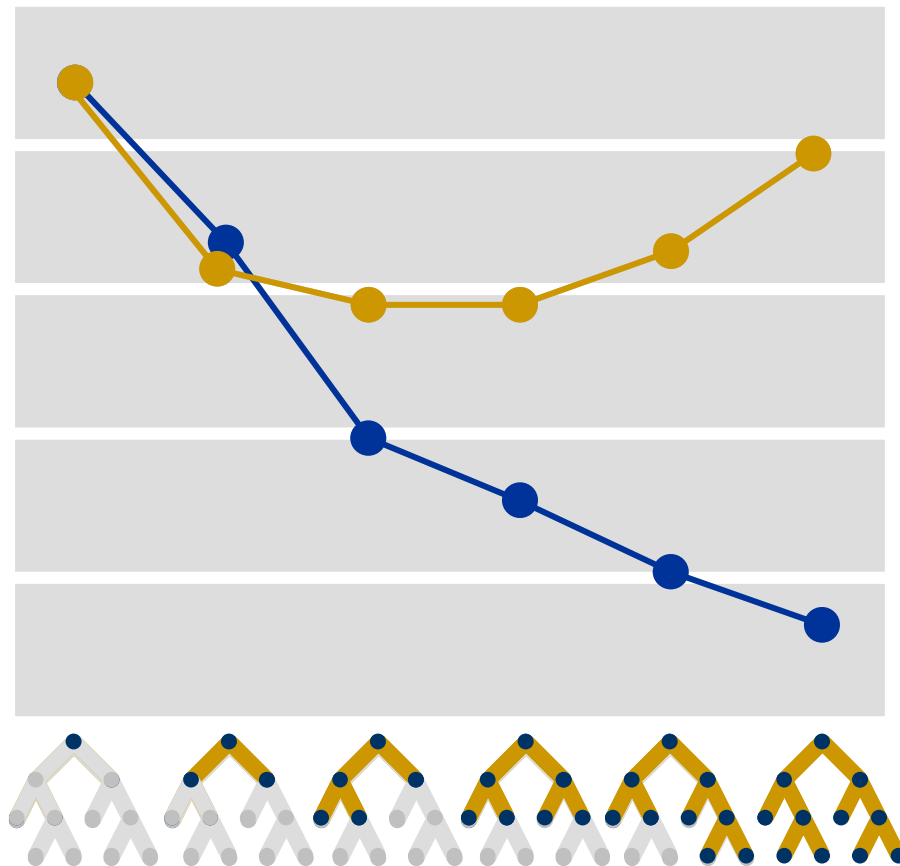


Create maximal tree.

Find optimal sub-trees.

Pick best sub-tree.

Pruning Strategy

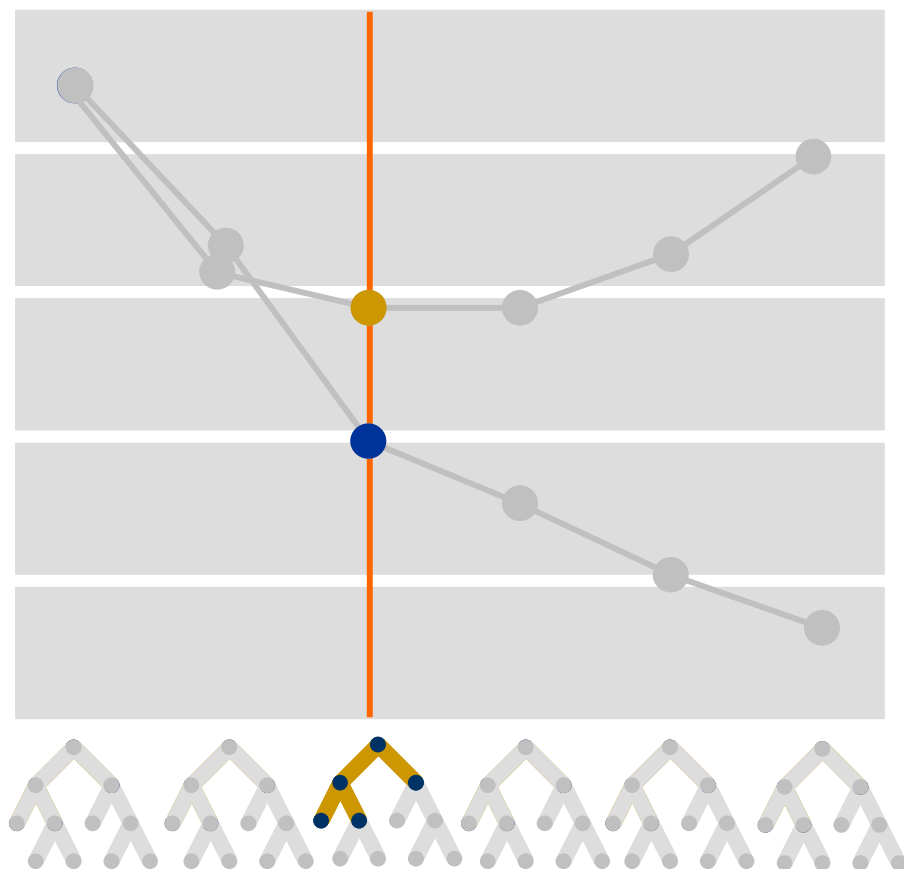


Create maximal tree.

Find optimal sub-trees.

Pick best sub-tree.

Pruning Strategy



Create maximal tree.

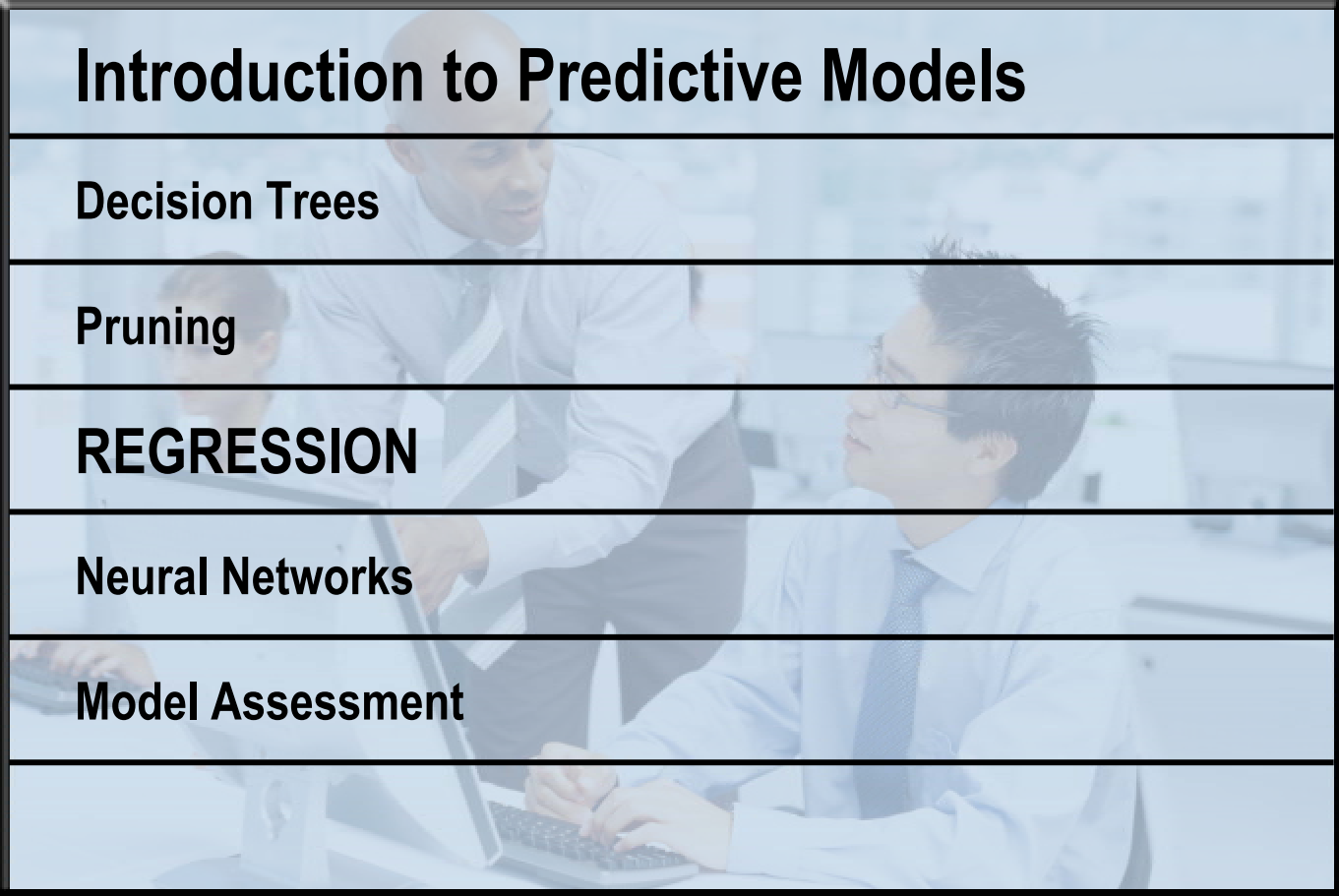
Find optimal sub-trees.

Pick best sub-tree.



Demo Pruning

Agenda



Introduction to Predictive Models

Decision Trees

Pruning

REGRESSION

Neural Networks

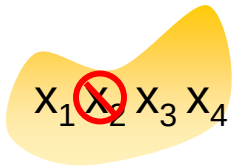
Model Assessment

Model Essentials – Regressions



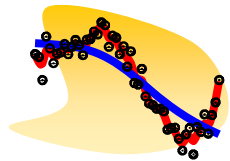
Predict new cases

**Prediction
formula**



Select useful inputs

**Sequential
selection**



Optimize complexity

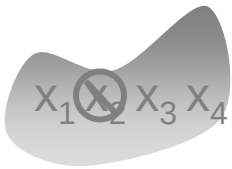
**Optimal sequence
model**

Model Essentials – Regressions



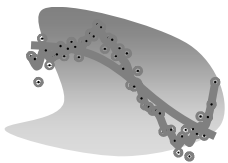
Predict new cases

**Prediction
formula**



Select useful inputs

Sequential
selection



Optimize complexity

Optimal sequence
model

Linear Regression Prediction Formula

$$\hat{y} = \hat{w}_0 + \hat{w}_1 x_1 + \hat{w}_2 x_2$$

prediction estimate

input measurement

intercept estimate *parameter estimate*

Choose intercept and parameter estimates to *minimize*.

squared error function

$$\sum_{\text{training data}} (y_i - \hat{y}_i)^2$$

Logistic Regression Prediction Formula

$$\log \left(\frac{\hat{p}}{1 - \hat{p}} \right) = \hat{w}_0 + \hat{w}_1 x_1 + \hat{w}_2 x_2 \quad \text{logit scores}$$

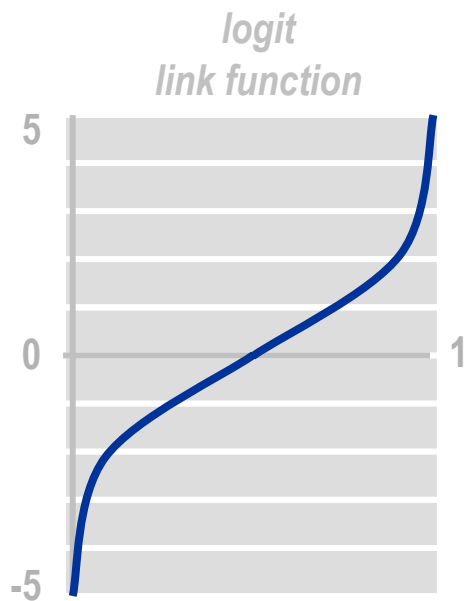
Choose intercept and parameter estimates to *maximize*.

log-likelihood function

$$\sum_{\substack{\text{primary} \\ \text{outcome} \\ \text{training cases}}} \log(\hat{p}_i) + \sum_{\substack{\text{secondary} \\ \text{outcome} \\ \text{training cases}}} \log(1 - \hat{p}_i)$$

Logit Link Function

$$\log \left(\frac{\hat{p}}{1 - \hat{p}} \right) = \hat{w}_0 + \hat{w}_1 x_1 + \hat{w}_2 x_2 \quad \text{logit scores}$$



Δx_i	consequence	
1	$\Rightarrow \text{odds} \times \exp(w_i)$	odds ratio
$\frac{0.69}{w_i}$	$\Rightarrow \text{odds} \times 2$	

doubling amount

Model interpretation

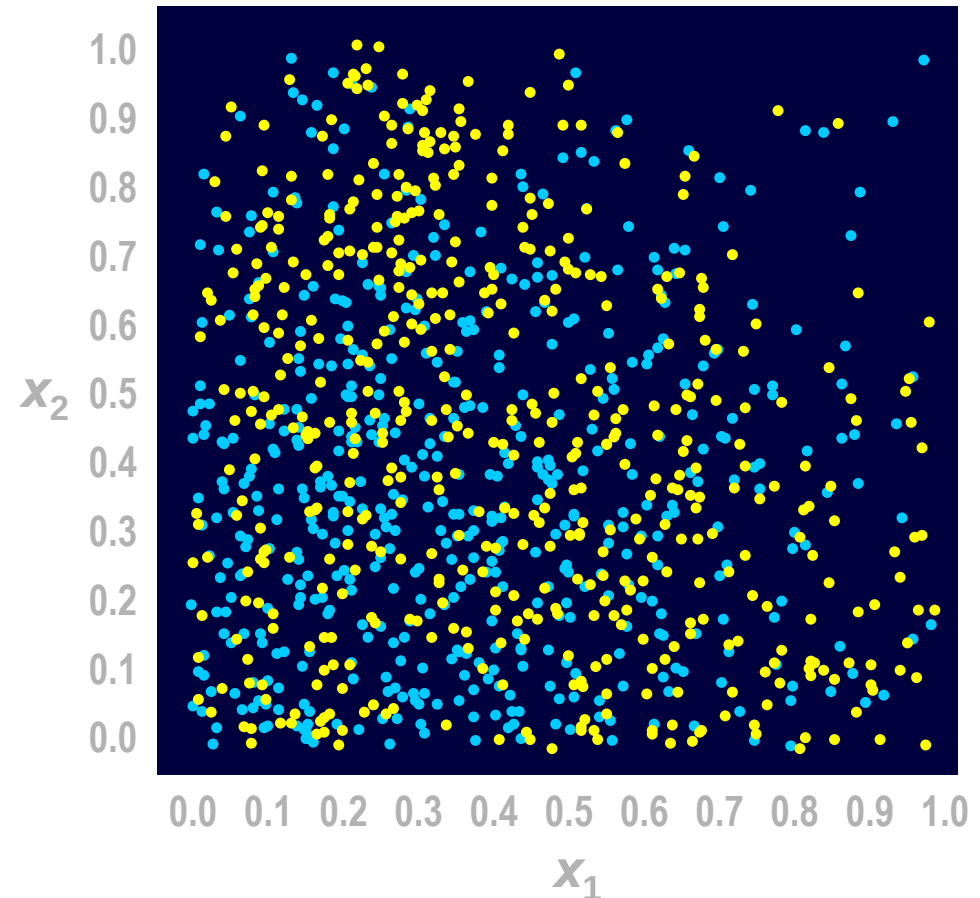
Simple Prediction Illustration – Regressions

logit equation

$$\text{logit}(\hat{p}) = \hat{w}_0 + \hat{w}_1 \cdot x_1 + \hat{w}_2 \cdot x_2$$

$$\hat{p} = \frac{1}{1 + e^{-\text{logit}(\hat{p})}}$$

logistic equation

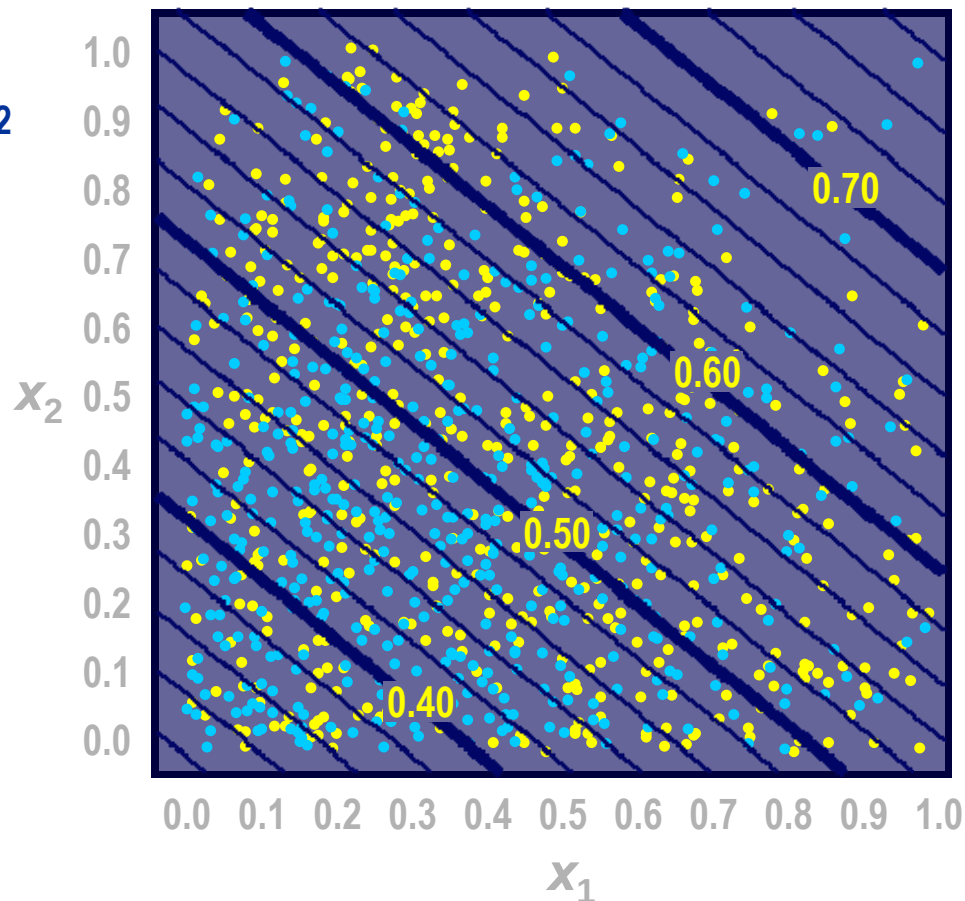


Prediction Estimates

$$\text{logit}(\hat{p}) = -0.81 + 0.92x_1 + 1.11x_2$$

$$\hat{p} = \frac{1}{1 + e^{0.81 - 0.92x_1 - 1.11x_2}}$$

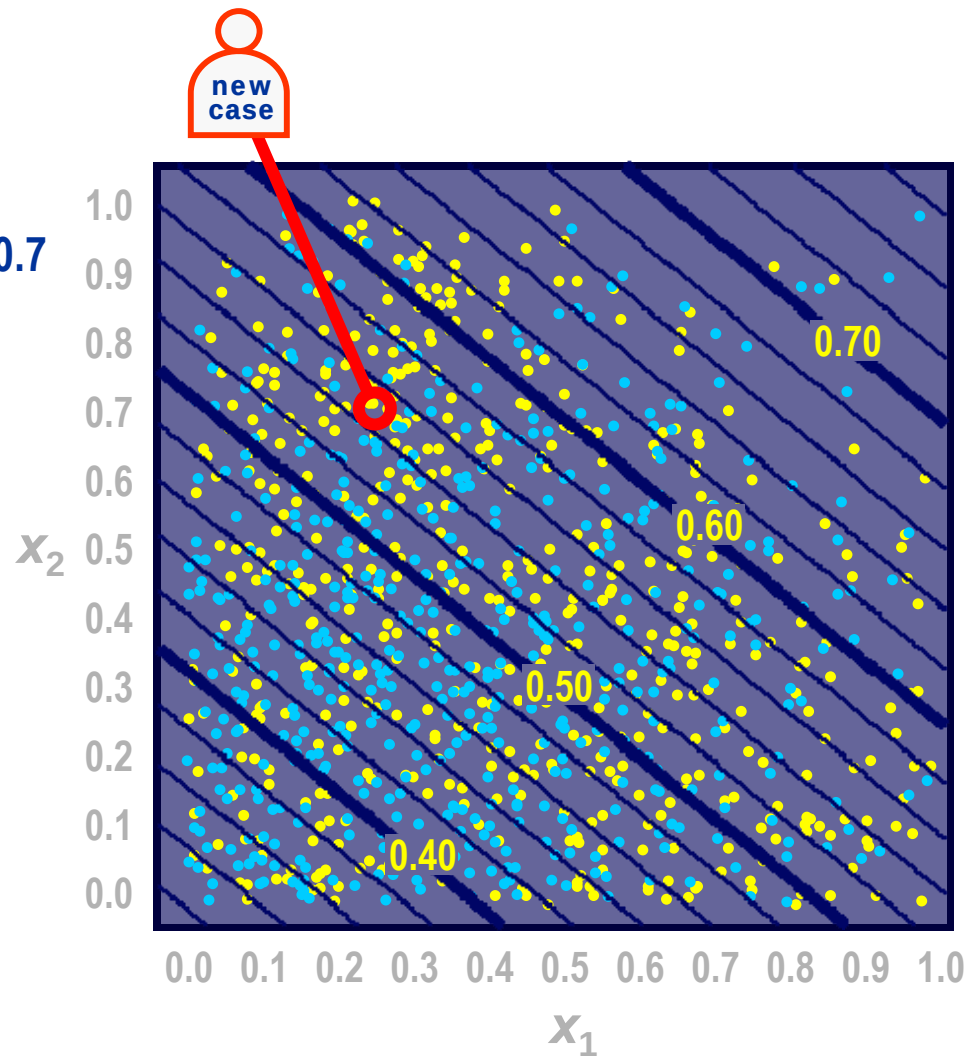
	x_1	x_2
odds ratio	2.5	3.0
doubling amount	0.75	0.62



Prediction Estimates

$$\text{logit}(\hat{p}) = -0.81 + 0.92 \cdot 0.3 + 1.11 \cdot 0.7$$

$$\hat{p} = \frac{1}{1 + e^{0.81 - 0.92 \cdot 0.3 - 1.11 \cdot 0.7}}$$



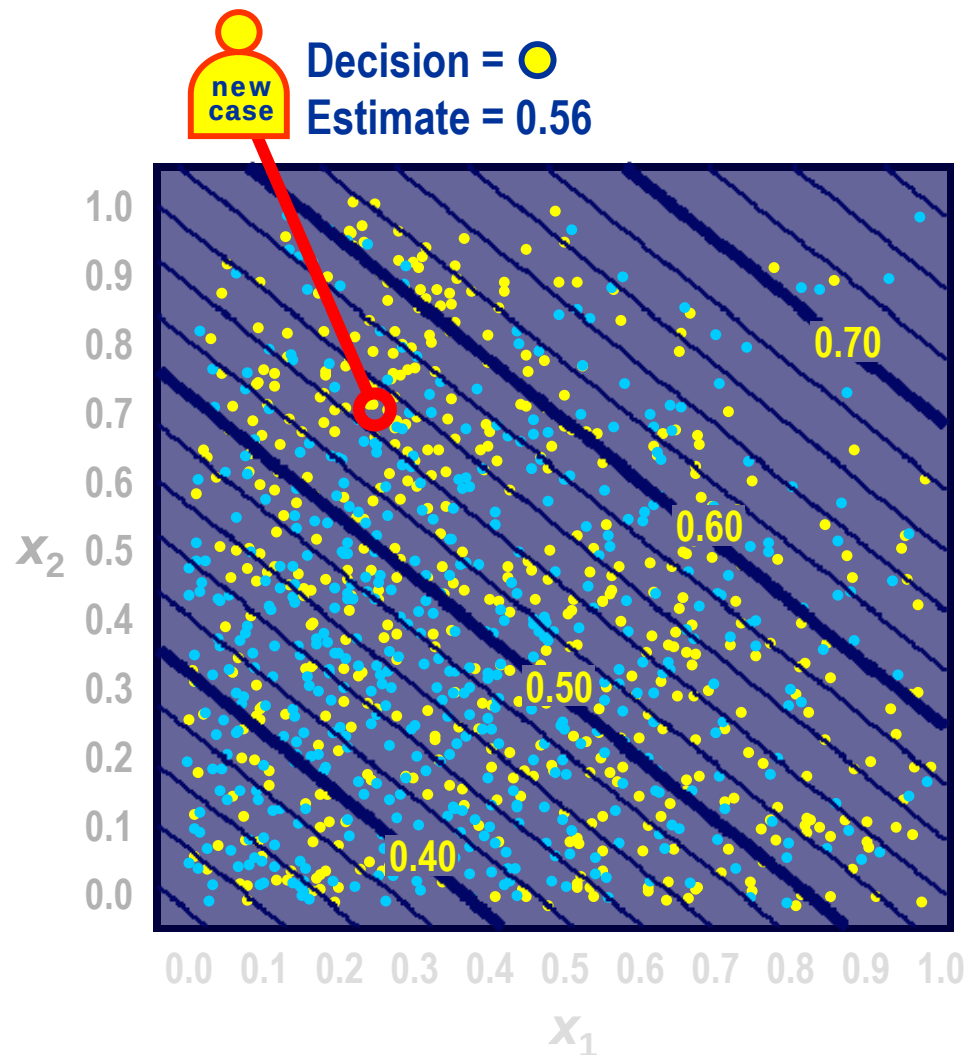
Prediction Estimates

logit score

$$\text{logit}(\hat{p}) = 0.104$$

$$\hat{p} = 0.56$$

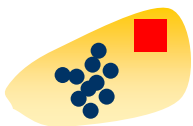
prediction estimate



Beyond the Prediction Formula



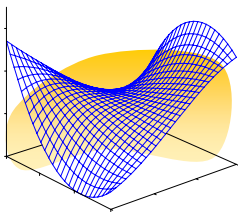
Missing values



Extreme or unusual values

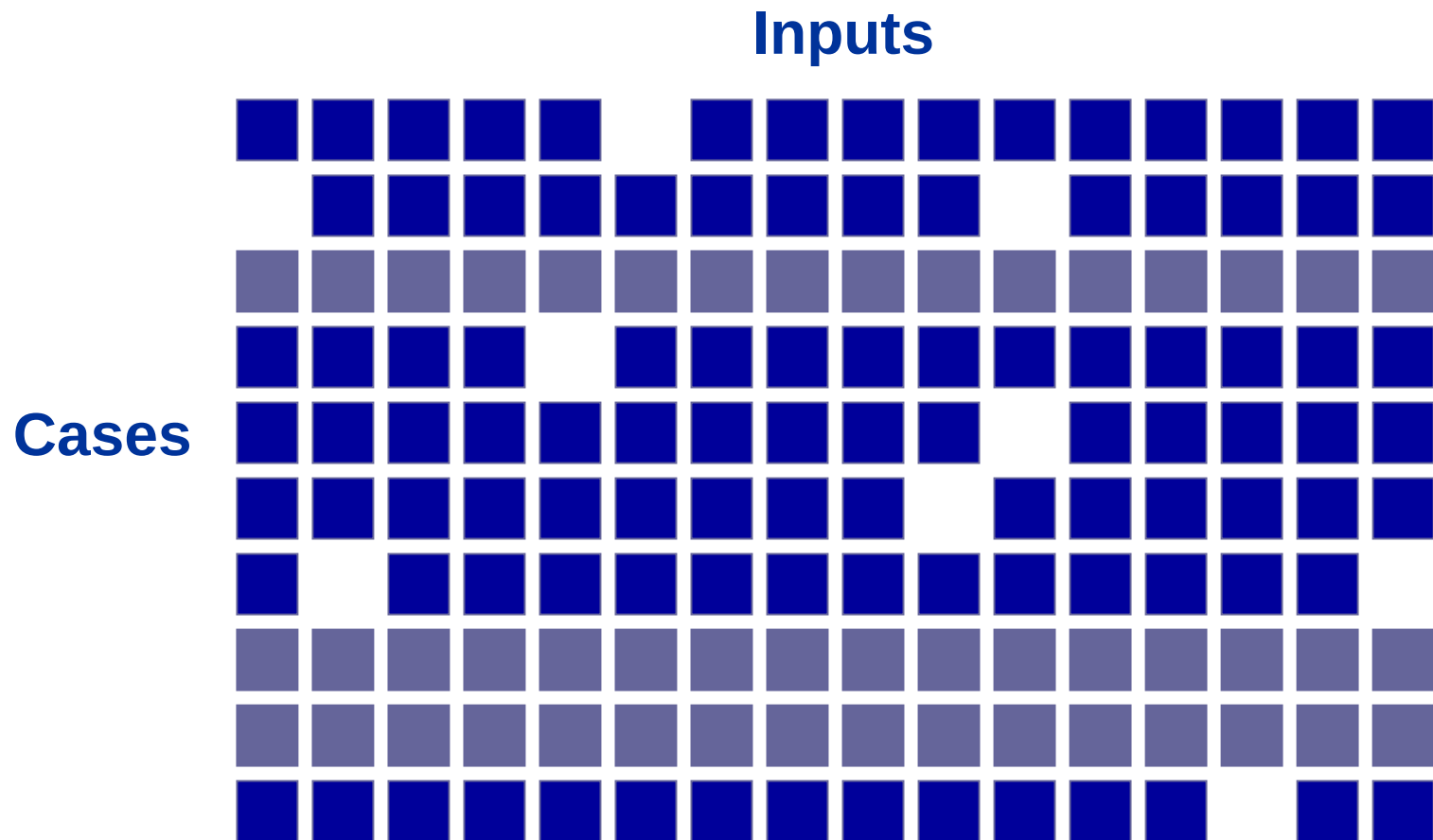


Non-numeric inputs



Nonlinearity and Non-additivity

Missing Values and Regression Modeling



Missing Values and Regression Modeling

		Inputs															
Cases		☐	☐	☐	☐	☐		☐	☐	☐	☐	☐	☐	☐	☐	☐	☐
			☐	☐	☐	☐	☐	☐	☐	☐		☐	☐	☐	☐	☐	☐
		☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒
		☐	☐	☐	☐		☐	☐	☐	☐	☐	☐	☐	☐	☐	☐	☐
		☐	☐	☐	☐	☐	☐	☐	☐	☐		☐	☐	☐	☐	☐	☐
		☐	☐	☐	☐	☐	☐	☐	☐		☐	☐	☐	☐	☐	☐	☐
		☐		☐	☐	☐	☐	☐	☐	☐	☐	☐	☐	☐	☐	☐	
		☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒
		☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒	☒
		☐	☐	☐	☐	☐	☐	☐	☐	☐	☐	☐	☐		☐	☐	

Missing Values and the Prediction Formula

Prediction Formula:

$$\text{logit}(p) = -2.1 + 0.072x_1 - 0.89x_2 - 1.24x_3$$

New Case:

$$(x_1, x_2, x_3) = (2, ?, -1)$$

Predicted Value:

$$\text{logit}(p) = -2.1 + 0.144x_1 - 0.8 ? + 1.24$$

Missing Value Causes



Not applicable



No match



Non-disclosure

Missing Value Remedies



Not applicable



No match



Non-disclosure

Synthetic distribution



Estimation

$$x_i = f(x_1, \dots, x_p)$$



Managing Missing Values

This demonstration illustrates how to impute synthetic data values and create missing value indicators.



Running the Regression Node

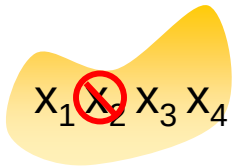
This demonstration illustrates using the Regression tool.

Model Essentials – Regressions



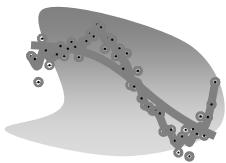
Predict new cases

Prediction
formula



Select useful inputs

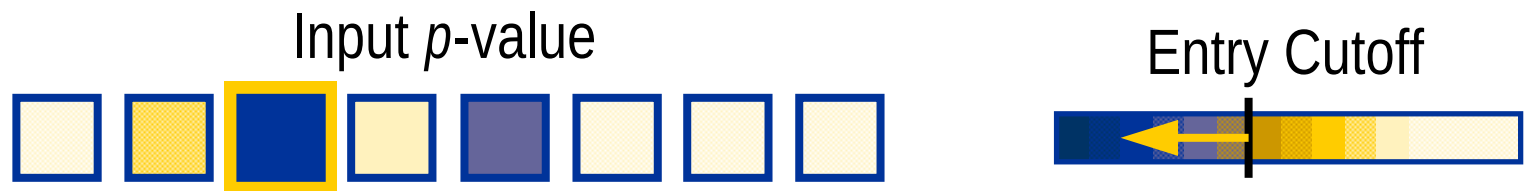
**Sequential
selection**



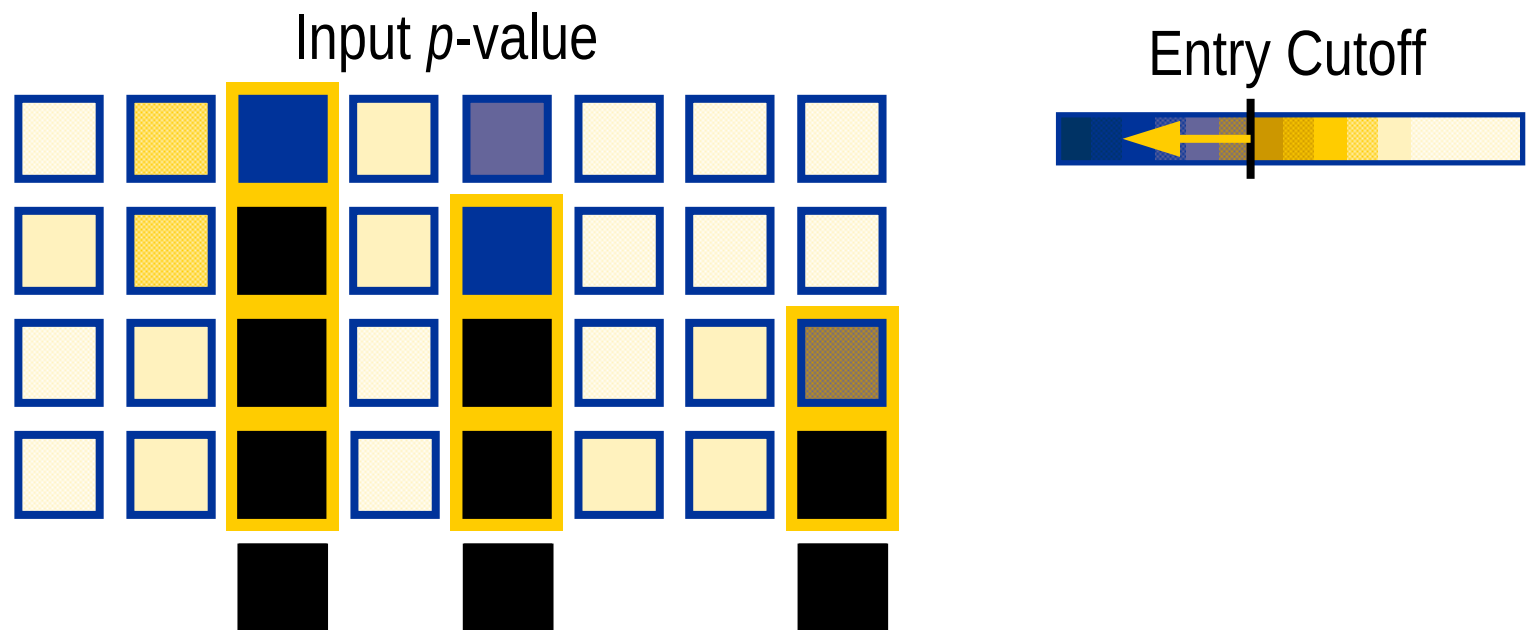
Optimize complexity

Optimal sequence
model

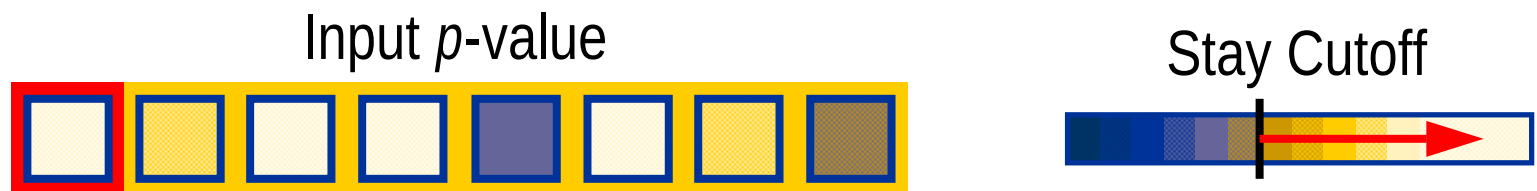
Sequential Selection – Forward



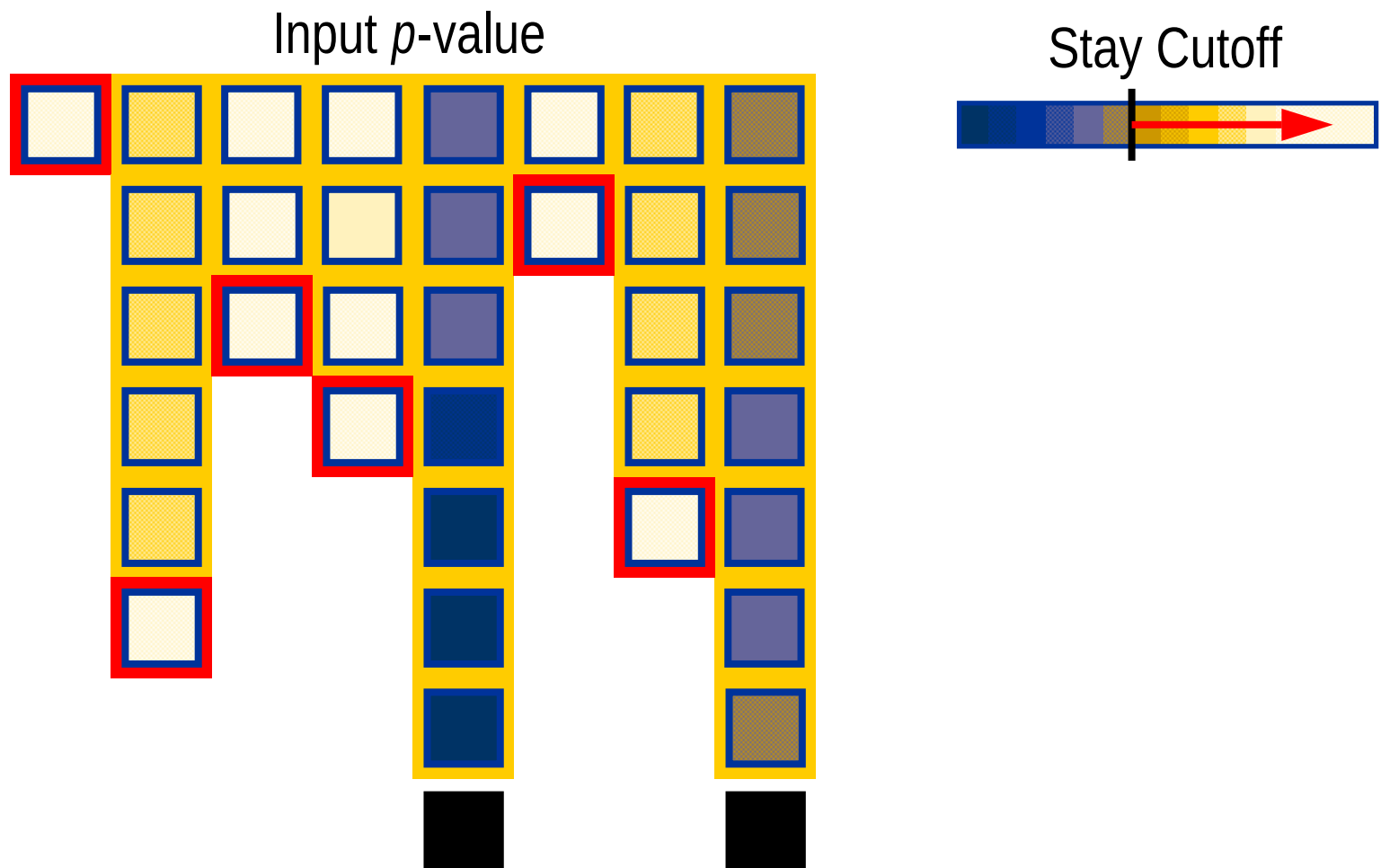
Sequential Selection – Forward



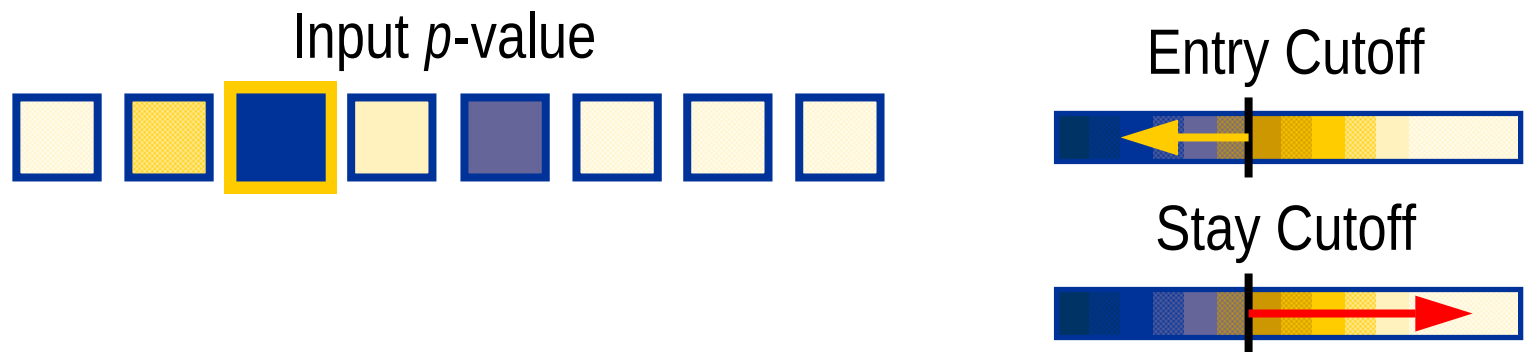
Sequential Selection – Backward



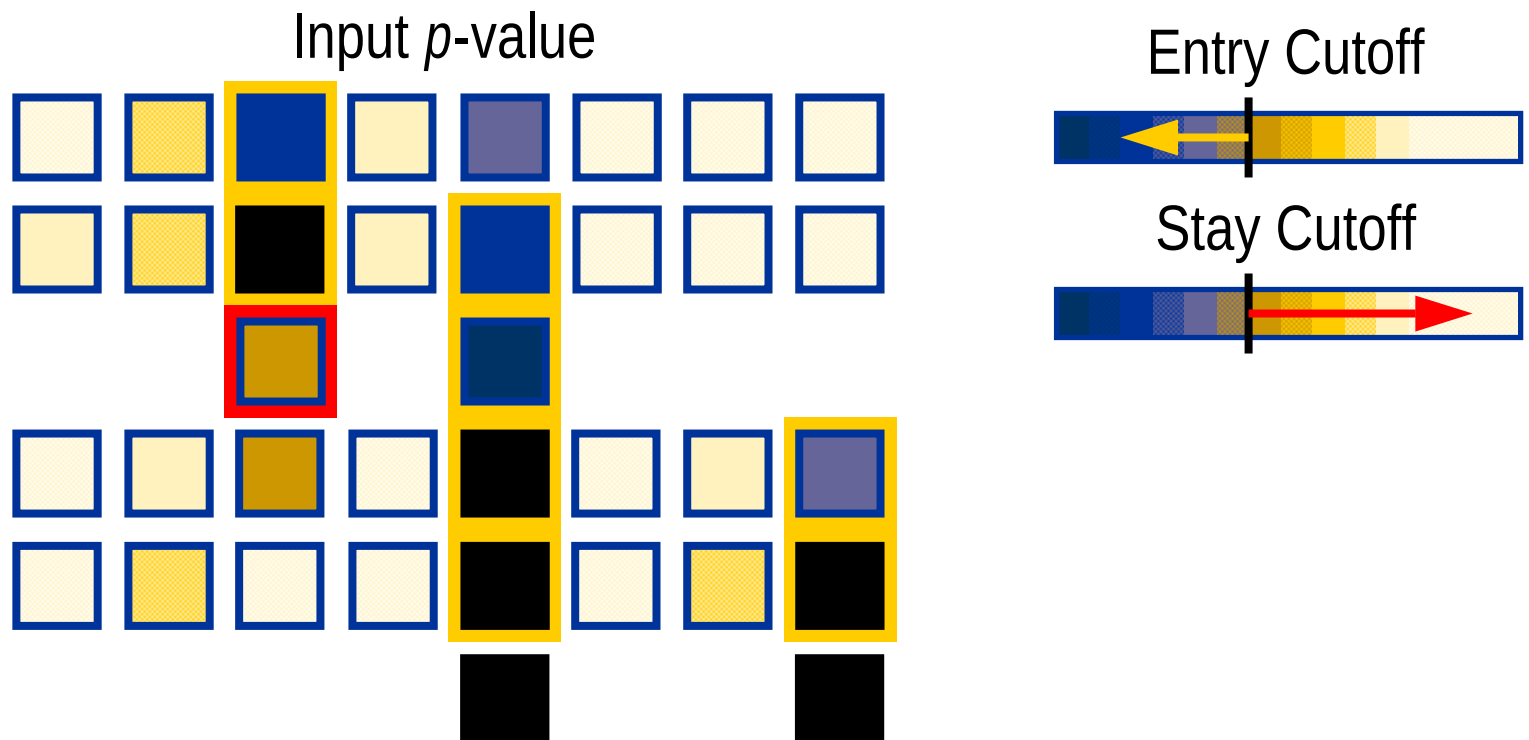
Sequential Selection – Backward



Sequential Selection – Stepwise



Sequential Selection – Stepwise

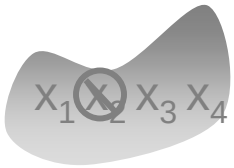


Model Essentials – Regressions



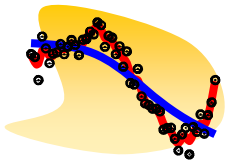
Predict new cases

Prediction
formula



Select useful inputs

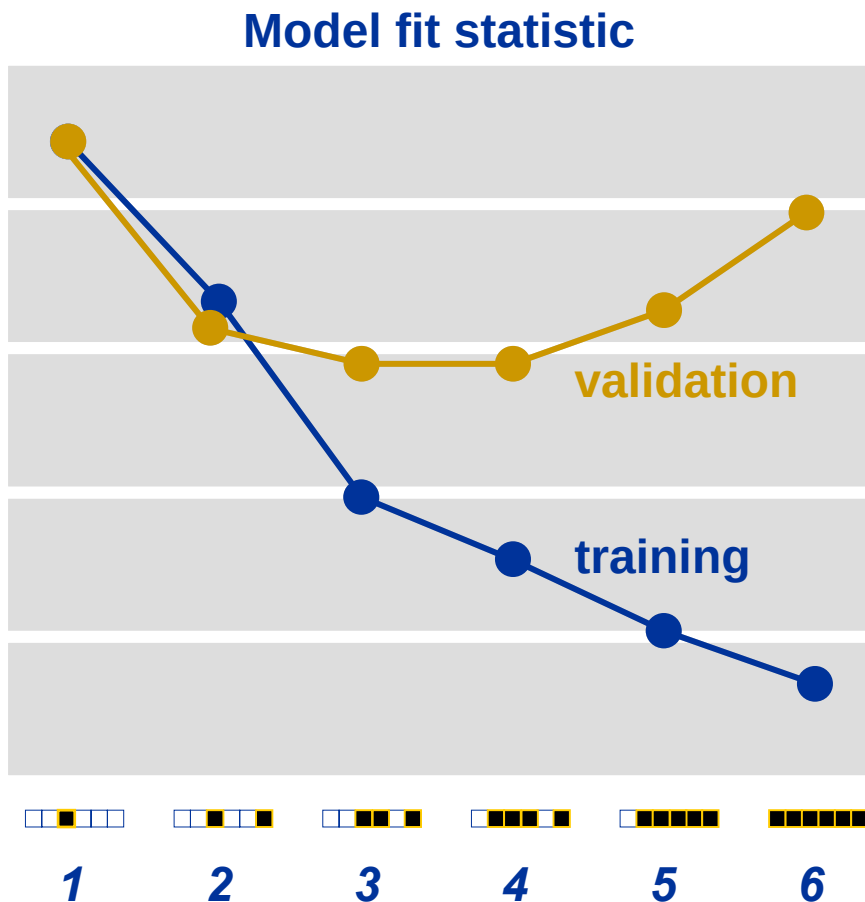
Sequential
selection



Optimize complexity

**Optimal sequence
model**

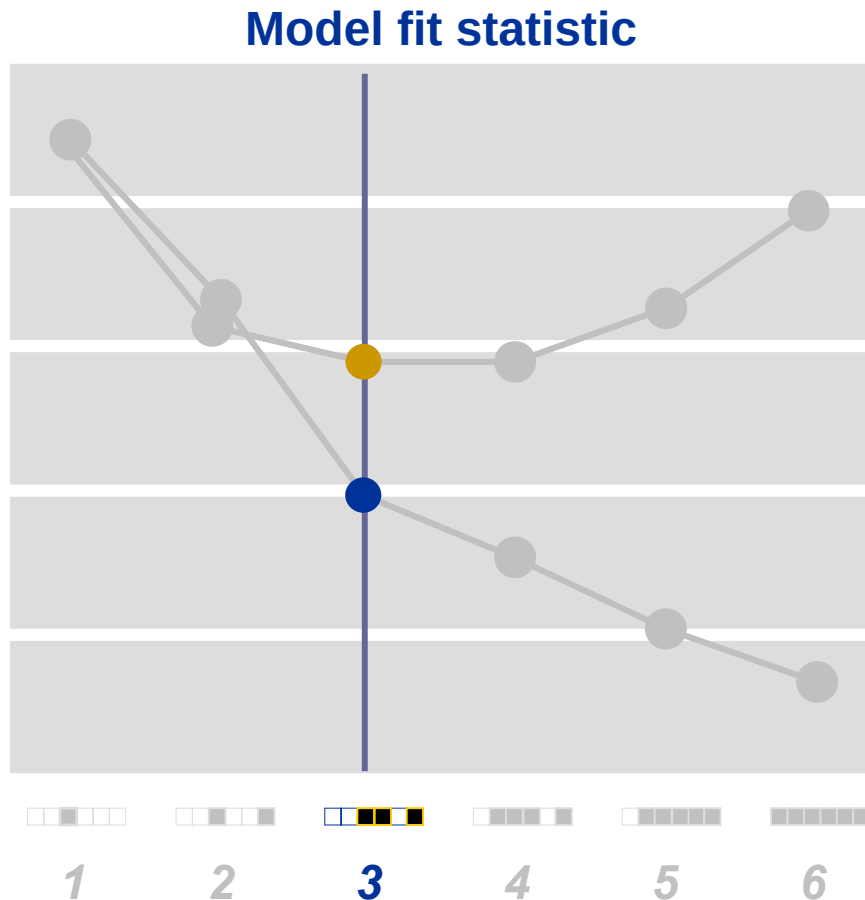
Model Fit versus Complexity



**Evaluate each
sequence step.**

Choose simplest
optimal model.

Select Model with Optimal Validation Fit



Evaluate each
sequence step.

**Choose simplest
optimal model.**

Agenda

Introduction to Predictive Models

Decision Trees

Pruning

Regression

NEURAL NETWORKS

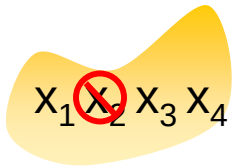
Model Assessment

Model Essentials – Neural Networks



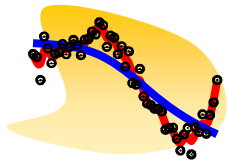
Predict new cases

**Prediction
formula**



Select useful inputs

None



Optimize complexity

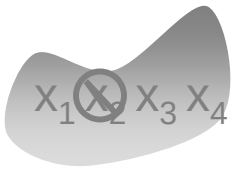
Stopped training

Model Essentials – Neural Networks



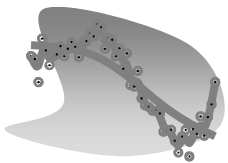
Predict new cases

**Prediction
formula**



Select useful inputs

None



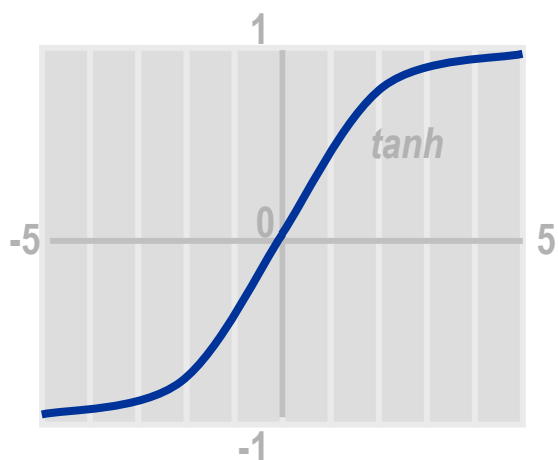
Optimize complexity

Stopped training

Neural Network Prediction Formula

$$\begin{array}{c} \text{prediction} \\ \text{estimate} \end{array} \hat{y} = \begin{array}{c} \text{hidden unit} \\ \hat{w}_{00} + \hat{w}_{01} H_1 + \hat{w}_{02} H_2 + \hat{w}_{03} H_3 \end{array}$$

$\hat{w}_{00}$ is the *bias estimate*, and $\hat{w}_{01}, \hat{w}_{02}, \hat{w}_{03}$ are *weight estimates*.



$$H_1 = \tanh(\hat{w}_{10} + \hat{w}_{11} x_1 + \hat{w}_{12} x_2)$$

$$H_2 = \tanh(\hat{w}_{20} + \hat{w}_{21} x_1 + \hat{w}_{22} x_2)$$

$$H_3 = \tanh(\hat{w}_{30} + \hat{w}_{31} x_1 + \hat{w}_{32} x_2)$$

*activation
function*

Neural Network Binary Prediction Formula

$$\log\left(\frac{\hat{p}}{1 - \hat{p}}\right) = \hat{w}_{00} + \hat{w}_{01} H_1 + \hat{w}_{02} H_2 + \hat{w}_{03} H_3$$

*logit
link function*

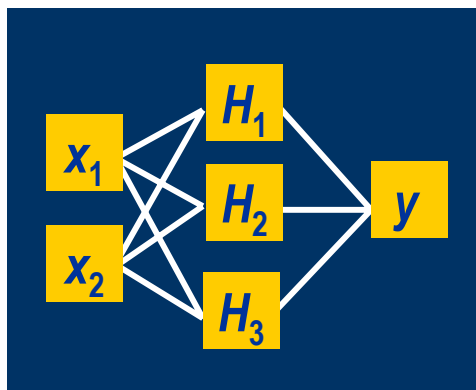
$$H_1 = \tanh(\hat{w}_{10} + \hat{w}_{11} x_1 + \hat{w}_{12} x_2)$$

$$H_2 = \tanh(\hat{w}_{20} + \hat{w}_{21} x_1 + \hat{w}_{22} x_2)$$

$$H_3 = \tanh(\hat{w}_{30} + \hat{w}_{31} x_1 + \hat{w}_{32} x_2)$$

Neural Network Diagram

$$\log\left(\frac{\hat{p}}{1 - \hat{p}}\right) = \hat{w}_{00} + \hat{w}_{01} H_1 + \hat{w}_{02} H_2 + \hat{w}_{03} H_3$$



input *hidden* *target*
layer *layer* *layer*

$$H_1 = \tanh(\hat{w}_{10} + \hat{w}_{11} x_1 + \hat{w}_{12} x_2)$$

$$H_2 = \tanh(\hat{w}_{20} + \hat{w}_{21} x_1 + \hat{w}_{22} x_2)$$

$$H_3 = \tanh(\hat{w}_{30} + \hat{w}_{31} x_1 + \hat{w}_{32} x_2)$$

Prediction Illustration – Neural Networks

logit equation

$$\text{logit}(\hat{p}) = \hat{w}_{00} + \hat{w}_{01}H_1 + \hat{w}_{02}H_2 + \hat{w}_{03}H_3$$

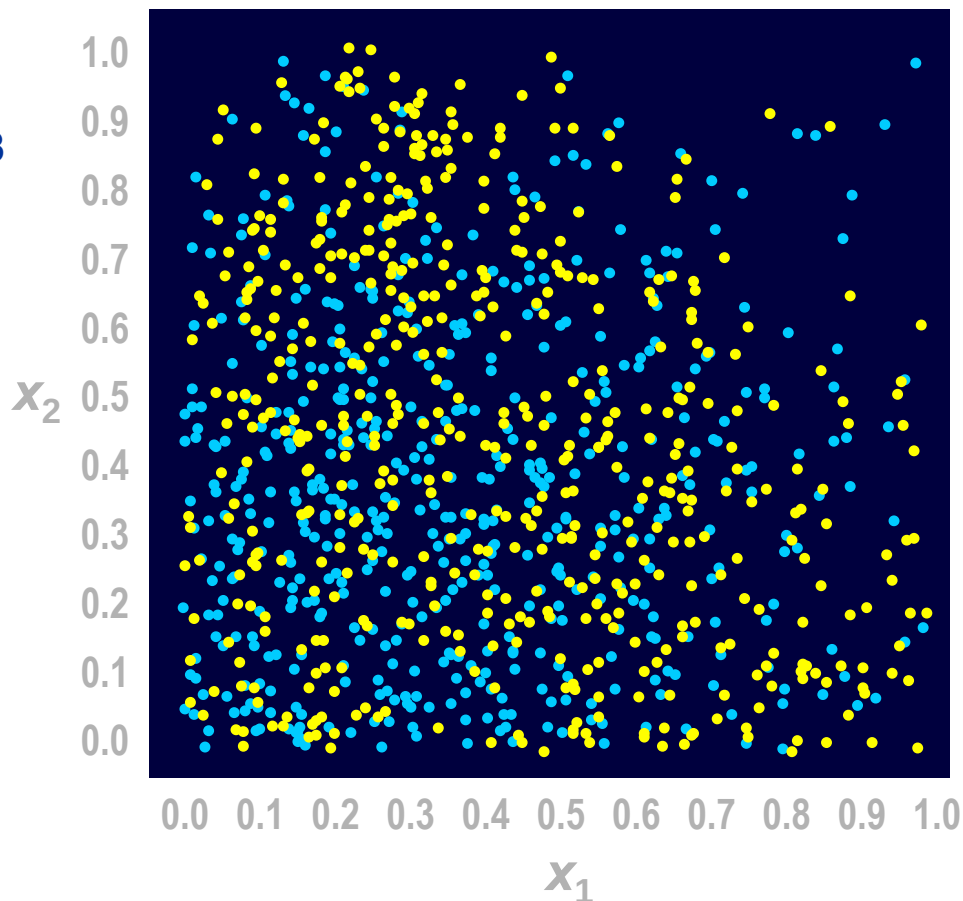
$$H_1 = \tanh(\hat{w}_{10} + \hat{w}_{11}x_1 + \hat{w}_{12}x_2)$$

$$H_2 = \tanh(\hat{w}_{20} + \hat{w}_{21}x_1 + \hat{w}_{22}x_2)$$

$$H_3 = \tanh(\hat{w}_{30} + \hat{w}_{31}x_1 + \hat{w}_{32}x_2)$$

$$\hat{p} = \frac{1}{1 + e^{-\text{logit}(\hat{p})}}$$

logistic equation



Prediction Estimates

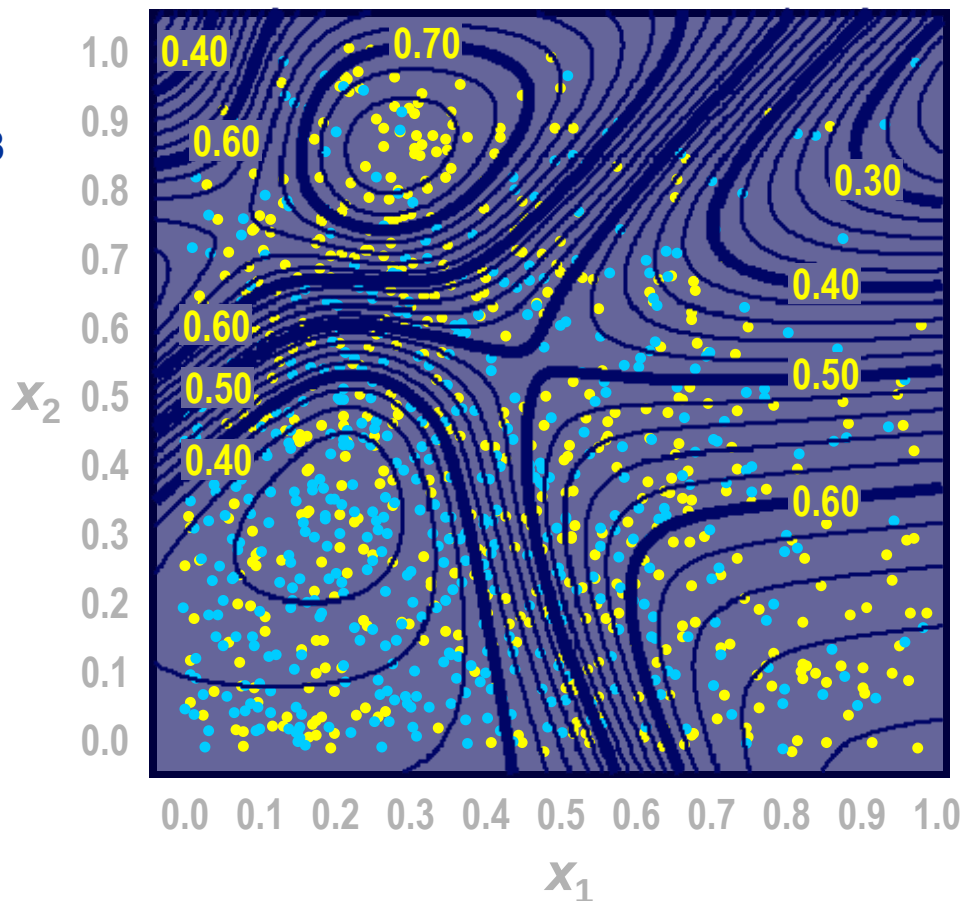
$$\text{logit}(\hat{p}) = -0.5 - 2.6H_1 - 1.9H_2 + .63 H_3$$

$$H_1 = \tanh(-1.8 - .25x_1 + 2.4x_2)$$

$$H_2 = \tanh(2.7 + 2.7x_1 - 5.3x_2)$$

$$H_3 = \tanh(-5.0 + 8.1x_1 + 4.3x_2)$$

$$\hat{p} = \frac{1}{1 + e^{-\text{logit}(\hat{p})}}$$



Prediction Estimates

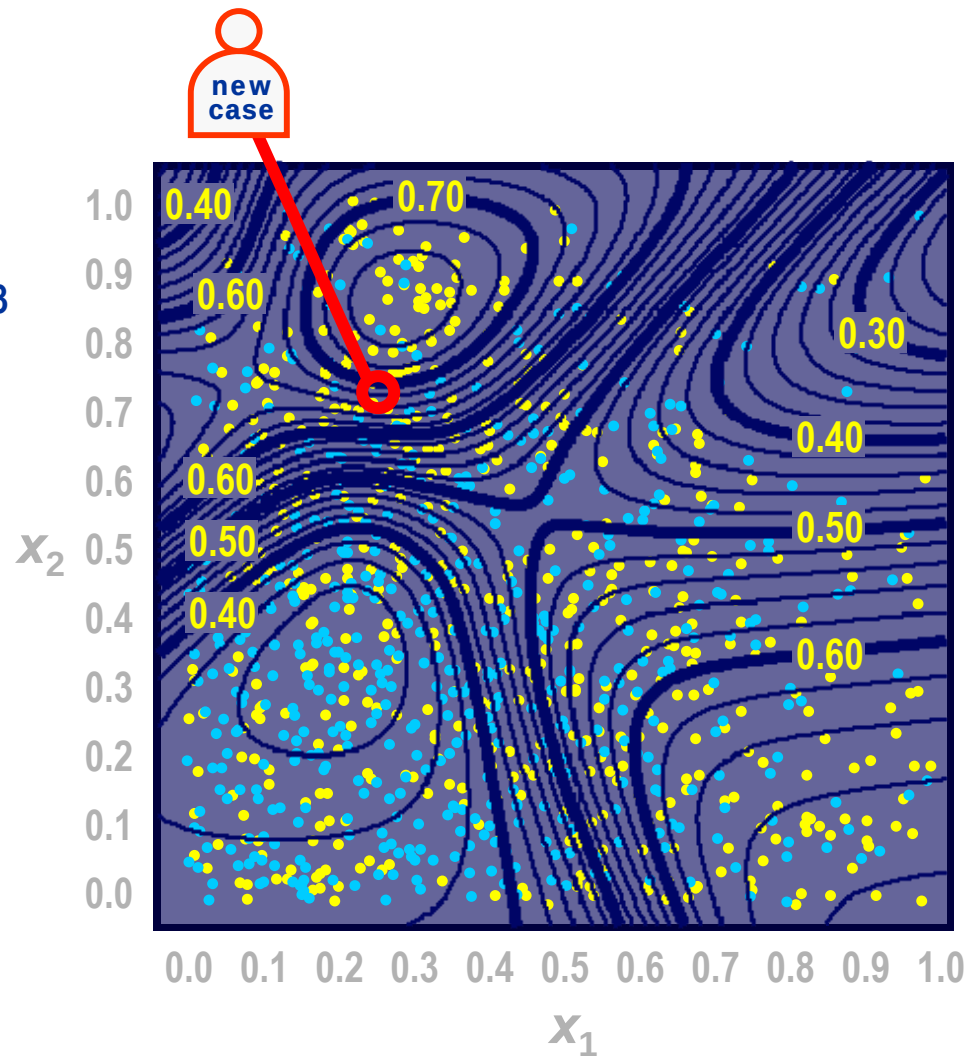
$$\text{logit}(\hat{p}) = -0.5 - 2.6H_1 - 1.9H_2 + .63 H_3$$

$$H_1 = -0.209$$

$$H_2 = -0.231$$

$$H_3 = 0.457$$

$$\hat{p} = \frac{1}{1 + e^{-\text{logit}(\hat{p})}}$$



Prediction Estimates

logit score

$$\text{logit}(\hat{p}) = 0.774$$

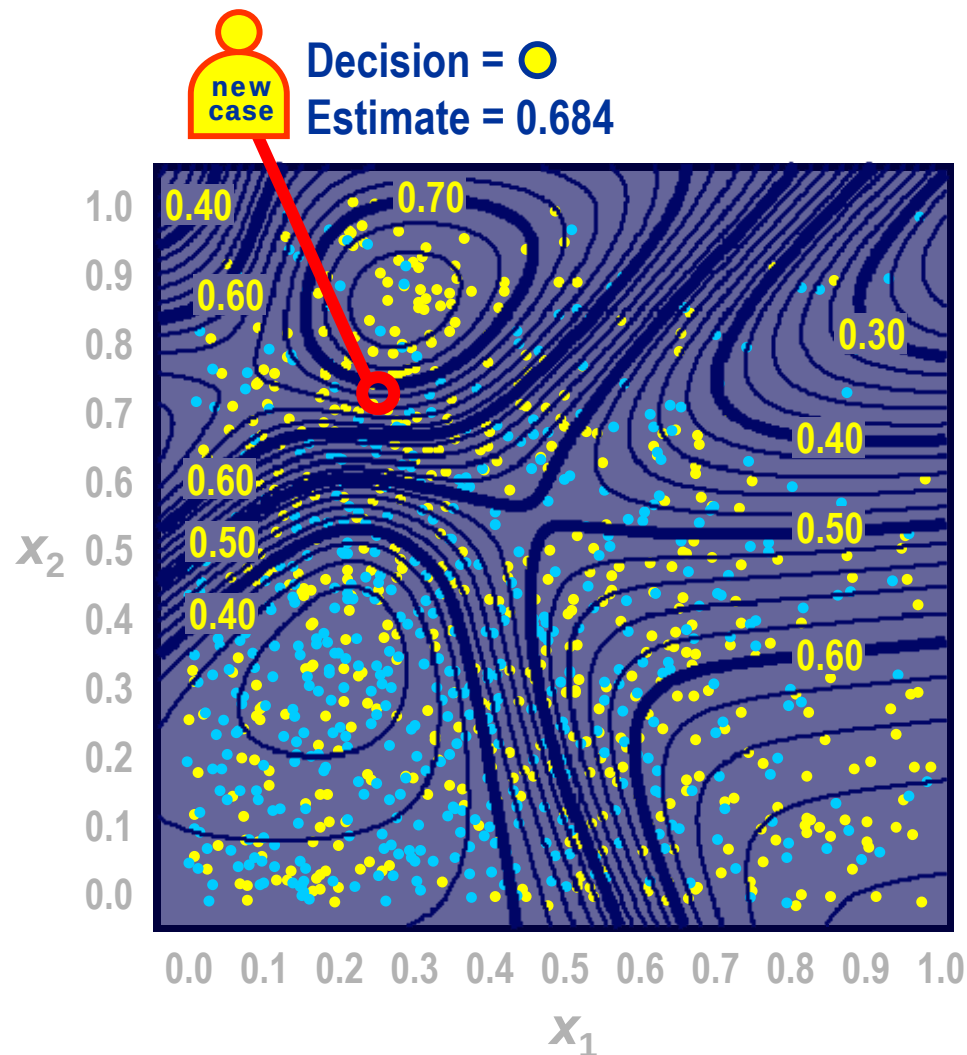
$$H_1 = -0.209$$

$$H_2 = -0.231$$

$$H_3 = 0.457$$

$$\hat{p} = 0.684$$

prediction estimate



Agenda

Introduction to Predictive Models

Decision Trees

Pruning

Regression

Neural Networks

MODEL ASSESSMENT

Assessment Types

The Model Comparison tool provides



Summary statistics

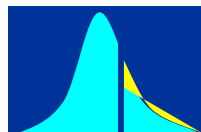


Statistical graphics

Summary Statistics Summary

Prediction Type

Statistic



Decisions

Accuracy / Misclassification
Profit / Loss
KS-statistic

1,2,3,...

Rankings

ROC Index (concordance)
Gini coefficient

$\hat{p} \approx E(Y)$

Estimates

Average squared error
SBC / Likelihood

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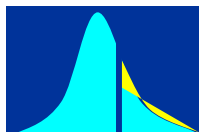
Comparing Models with Summary Statistics

This demonstration illustrates the use of the Model Comparison tool, which collects assessment information from attached modeling nodes and enables you to easily compare model performance measures.

Statistical Graphics Summary

Prediction Type

Statistic



Decisions

1,2,3,...

Rankings

$\hat{p} \approx E(Y)$

Estimates

Sensitivity charts

Response rate charts