

# Generalized Linear Models (ST425A)

(Advanced level course, 7.5 hec, Aut. 2019)

## Examnation (Part 2)

Gebrenewus Ghilagaber (Professor & Head)  
Department of Statistics, Stockholm University

- **Date and time:** Monday 30 September 2019, 13:00 - 15:00
- **Permitted facilities:** Pocket calculator and attached R- and SAS-codes.
- **Return of exam:** Not yet decided (information will be sent via e-mail or athena).
- **Instructions:**
  - The total amount of points for this part of the exam is 20.
  - The minimum requirement to pass this part of examination is 10 points.
  - Solutions to each question should be detailed enough and well-motivated in order to get full points.

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The table below presents the results of a survey on ideal number of children (grouped into 3 increasing categories) among 3663 women cross classified by their education (3 levels) and residence (2 levels).

Education	Residence	Ideal # children		
		$\leq 2$	3 - 5	$> 5$
None	Urban	218	200	248
	Rural	731	643	532
Primary	Urban	220	143	121
	Rural	134	44	18
Secondary or above	Urban	250	94	35
	Rural	22	6	4

- a) Fit an appropriate model with *Ideal # children* as response variable and *Education* as explanatory variable.
- b) Repeat (a) with *Education* and *Residence* as explanatory variables.
- c) Use the model-deviances in (a) and (b) to suggest which model is more adequate.
- d) Do the results in (a) and (b) indicate you need to add an interaction term (between *Education* and *Residence*) to the model in (b)?
- e) Interpret your final results on the effect of *Education* and *Residence* on ideal children ever born

Summarize your results in a form of a report that includes choice of a model (with justification), the fitted model, and overall comments on your results (estimates and test statistics). Attach relevant SAS or R codes, tables and figures as appendices.

## Generalized Linear Models 2019: R- and SAS Commands

Packages Used
car ResourceSelection aod nnet MASS VGAM vcd mcprofile lmtest

Description	Command
Simple/multiple linear regression	<code>lm(formula, data)</code>
One-way / Two-way ANOVA	<code>aov(formula , data)</code>
Type I SS	<code>anova(model)</code>
Type II or III SS	<code>Anova(model , type="II")</code> <code>Anova(model , type="III")</code>
Binary regression	<code>glm(cbind(y,n-y)~ , family=binomial(link="logit"),data)</code>  <code>link=c("logit ","probit ","cloglog")</code>
Odds ratio estimates (model with interaction)	<code>predict.glm(model, newdata=data.frame(x1=c(),x2=factor()),se.fit=TRUE)</code>
Multinomial logistic regression	<code>multinom(formula,data,weights)</code>
Proportional odds models	<code>polr(formula,data,weights,Hess=TRUE,method="logistic")</code> <code>method = c("logistic", "probit", "cloglog", "cauchit")</code>  <code>vglm(formula=formula, family=cumulative (link="logitlink",parallel=T, reverse=F), weights,data)</code>
Adjacent-Category model (with proportional odds assumption)	<code>vglm( formula, family=acat (link="loglink", parallel=T, reverse=F), weights,data)</code>

<p>Continuation ratio (with proportional odds assumption)</p>	<p>vglm(formula, family=sratio(link="loglink", parallel=T, reverse=F), weights, data)</p>	<p>Log-linear models</p> <p>glm(formula, family=poisson(link="log", data)</p> <p>exp(confint(mcpofie(model, CM=matrix(C,1)))</p> <p>where C is the contrast matrix</p>	<p>Standardized residuals</p> <p>rsstandard(model)</p> <p>Jack-knife/studentized residuals</p> <p>cooks.distance(model)</p> <p>leverages</p> <p>residuals(model, type="pearson")</p> <p>residuals(model, type="deviance")</p>	<p>Akaike's information criterion</p> <p>AIC(model)</p> <p>Bayesian information criterion</p> <p>BIC(model)</p> <p>Log likelihood</p> <p>loglik(model)</p> <p>deviance(model)</p>	<p>Likelihood ratio test</p> <p>anova(model1, model2, test="Chisq")</p> <p>Shapiro-Wilk Test</p> <p>shapiro.test()</p> <p>Brush Pagan Test</p> <p>bp.test(model)</p> <p>Tests for homogeneity of variance across groups</p> <p>fligner.test(y~group, data)</p> <p>leveneTest(y~group, data)</p> <p>Hosmer-Lemeshow's goodness of fit</p> <p>hoslem.test(y, fitted(model), g=)</p> <p>Wald test</p> <p>wald.test(b = coef(model), Sigma = vcov(model), Terms =)</p> <p>Testing for single/joint effects of covariates/factors</p> <p>linearHypothesis(M1, c("coef1" = "coef2"), test="Chisq")</p> <p>linearHypothesis(M1, c("coef1" = "0"), test="Chisq")</p> <p>linearHypothesis(M1, c("coef1" = "coef2"), test="Chisq")</p> <p>assocstats(H)</p>	<p>Confidence intervals for parameter estimates</p> <p>confint()</p> <p>confint.default()</p>
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Relevel/order factors	relevel(x, ref="") factor(x, levels=unique(x)) factor(x, ordered=T)
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Description	Command
<p>Simple/multiple linear regression</p> <p>anova</p>	<pre>proc glm data = data plots=diagnostics;   model formula/ SS1 SS2 SS3 solution; means x;   lsmeans x / adjust = tukey cl;   output out = estlm p= phat r=resid student = stresid   cookd=cooks dffits = DFIT h = hat_matrix;   class A (ref = 'A1') B (ref = 'B1');</pre>
<p>Binary regression</p> <p>Odds ratio estimates (model with interaction)</p>	<pre>proc logistic data = dataset;   model formula /link=LOGIT (orPROBIT or CLOGLOG)   aggregate scale = none influence;   effectplot fit/obs;   output out=tablename pred=logit (or probit or ploglog)   resdev = resdev reschi= Pearson stdev = stdev   stdevschl = stdPearson; run;   EFFECTPLOT FIT (PLOTBY = name of CLASS variable)/obs;   ODDSRAATIO name of class var;</pre>
<p>Multinomial logistic regression</p> <p>cumulative logit model</p> <p>Adjacent-Category model (with proportional odds assumption)</p> <p>Continuation ratio (with proportional odds assumption)</p>	<pre>ods graphics on;   proc logistic data=dataset;   freq frequency;   class var1 (ref=" param=ref) var2(ref=" param=ref);   model response (ref='baseline')=var1 var2/ link = glogit;   effectplot interaction (plotby=var1)/polybar;   oddsratio var;   run;   model / LINK = clogit scale=none aggregate;   effectplot interaction(plotby=covariate);   output out=pred predprobs= i predprobs = c;</pre>
<p>Contingency table</p> <p>Log-linear models</p>	<pre>proc freq data = dataset order = data;   weight n;   tables var1*var2 / chisq expected nopcent nocol nocum   norow; run;   proc genmod data = data;</pre>

<pre>class var1 (ref = 'reference group name') var2 (ref = ' reference group name"); model formula / dist = poisson obstats type3; ods output obstats = test1 (keep = frequency type site pred Xbeta std Reschi Resdev); run; estimate 'RR' var1 1 0 -1 0 var1*var2 1 0...0 /e ;</pre>	<p>Rate ratio + CI</p>
	<p>Standardized residuals Jack-knife/studentized residuals Cooks distance Leverages Pearson residuals Deviance residuals</p>
	<p>Alkaike's information criterion Bayesian information criterion Log likelihood deviance</p>
<pre>proc logistic data = data; model formula / link=logit lackfit; run;</pre>	<p>Likelihood ratio test Shapiro-Wilk Test Breush Pagan Test Tests for homogeneity of variance across groups Hosmer-Lemeshow's goodness of fit Wald test Testing for single/joint effects of covariates/factors Pearson chi-squared test for independence</p>
	<p>Confidence intervals for parameter estimates Relevel/order factors</p>

