

## BASIC STATISTICS FOR ECONOMISTS, STE101. EXAM

Department of statistics Edgar Bueno 2024–05–30

**Time:** 14:00 — 19:00

Approved aid: Hand-held calculator with no stored text, data or formulas

Provided aid: Formula Sheet and Probability Distribution Tables, returned after the exam.

#### Problems 1 - 12: Multiple choice questions (max 60 points):

- A total of 12 multiple choice questions with five alternative answers per question one of which is the correct answer. Mark your answers on the attached **answer form**.
- Marking more than one alternative will result in zero points for that question.
- Each correct answer is worth 5 points.
- Written solutions should <u>not</u> be submitted; only your answers on the answer form will be considered in the assessment and final grading.

### Problems 13 — 14: Complete written solutions (max 40 points):

- Use only the provided answer sheets when submitting your solutions and answers.
- For full marks, clear, comprehensive and well-motivated solutions are required. Unclear and unexplained solutions will result in point deductions even if the final answer is correct.
- Check your calculations and solutions before submitting. Careless mistakes will result in unnecessary point deductions.

The maximum total number of points is 60 + 40 = 100. At least 50 points are required to pass (grades A-E). The grading scale is as follows:

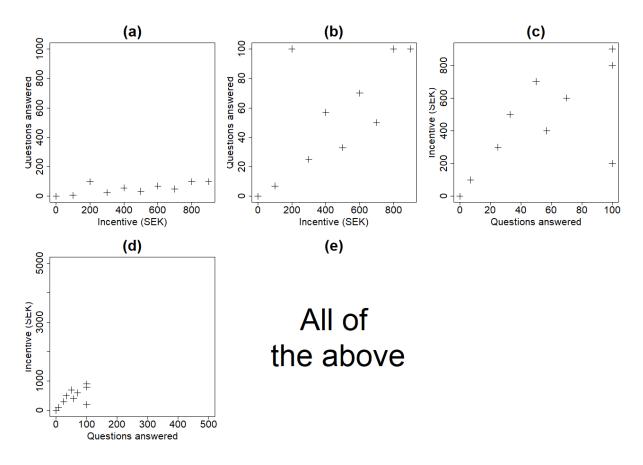
**NOTE:** Fx and F are failing grades that require re-examination. Students who receive the grade Fx or F cannot supplement extra assignments for a higher grade.

# Part one. Multiple choice

1. A researcher in survey methodology is studying the effect of incentives on item nonresponse. To this end she has selected a sample of ten individuals, offered them different amounts of money and submitted them to a long questionnaire. Then she has measured how many questions they answer before they get tired and decide to stop. Table 1 shows the results.

Table 1: Incentives offered to and number of questions answered by a sample of ten respondents

Which of the following is a scatter plot that adequately represents the measurements in Table 1?



- 2. Which of the following sentences is **not** correct regarding the *cumulative probability distribution* of a discrete random variable X,  $F_X(x)$ :
  - (a)  $\lim_{x\to\infty} F_X(x) = 0$ ;
  - (b)  $\lim_{x \to -\infty} F_X(x) = 0;$
  - (c) it is a non-decreasing function;
  - (d) it takes values between 0 and 1, i.e.  $0 \le F_X(x) \le 1$  for all x;
  - (e) it is a step function.

- 3. It is known that the weight of male african lions has an expectation of 204 kg and a standard deviation of 18 kg. A researcher will select a random sample of 10 male african lions. Which of the following is **correct**:
  - (a) the variance of the sample will be 324 kg<sup>2</sup>;
  - (b) the mean of the sample will be 204 kg;
  - (c) the sample mean follows a normal distribution;
  - (d) the sample mean has an expected value of 204 kg;
  - (e) the sample mean has a variance of 324 kg<sup>2</sup>.
- 4. The owner of an electronic store wants to verify the hypothesis that 60%, 30% and 10% of the customers buy, respectively, cell phones of the brands A, B and C. Which of the following is an appropriate method to this end:
  - (a) multiple linear regression;
  - (b) time-series analysis;
  - (c) goodness-of-fit test;
  - (d) simple linear regression;
  - (e) test of independence.
- 5. A researcher has asked the thirteen married men in a small community about the brideprice they had to pay to the bride's family when they got married. The brideprice values (in USD) are

 $20000 \quad 3000 \quad 10000 \quad 20000 \quad 13000 \quad 0 \quad 31000 \quad 20000 \quad 63000 \quad 8000 \quad 3000 \quad 12000 \quad 4000$ 

What is the **interquartile range** of the brideprice?

- (a) -9500;
- (b) 9500;
- (c) 11000;
- (d) 16500;
- (e) 63000.
- 6. An ice-cream shop offers 10 different flavors. How many combinations of 2 scoops can be made if the order is important and no flavor can be used more than once?
  - (a) 20;
  - (b) 45;
  - (c) 55;
  - (d) 90;
  - (e) 100.

7.	In a card game, the player has three possible outcomes: win, tie or lose. If the player wins
	(which happens with probability 0.19), he gets two dollars; if the player loses (which happens
	with probability 0.47), he loses one dollar; in the case of a tie, the player neither wins nor loses
	any money. What is the expected amount of money of the player at the end of one game?

- (a) -0.39;
- (b) -0.09;
- (c) 0.00;
- (d) 0.33;
- (e) 1.00.
- 8. The amount of money spent on clothing by students on Stockholm University during 2023 can be modeled by a normal distribution with expected value of 1200 and variance of 40 000. The amount of money spent on course literature can be modeled by a normal distribution with expected value of 800 and variance of 18 000. The covariance between money spent on clothing and course literature is  $-24\,000$ . What is the probability that one student chosen at random spent more than 2000 on clothing plus course literature?
  - (a) 0;
  - (b) 0.0967;
  - (c) 0.5;
  - (d) 0.25;
  - (e) 1.
- 9. One week before the local elections of a city, a poll is carried out by selecting a random sample of 100 voters. The proportion of individuals in the sample who will vote for the candidate of the party A is 0.4. A 99% confidence interval for the proportion of individuals who will vote for this candidate on the elections is:
  - (a) (0%, 99%);
  - (b) (27.4\%, 52.6\%);
  - (c) (30.4%, 49.6%);
  - (d) (39.4%, 40.6%);
  - (e) (39.5%, 40.5%);
- 10. One week before the local elections of a city, a candidate, Mrs. B, believes that more than 30% of the voters support her. In order to verify her claim, the campaign has selected a sample of 100 voters. 37 out of the 100 voters in the sample claim that they will vote for Mrs. B. The value of the statistic for testing the alternative that the proportion of voters for Mrs. B is larger than 30% is:
  - (a) 1.45;
  - (b) 1.66;
  - (c) 1.98;
  - (d) 14.50;
  - (e) 30.03;

- 11. Fitting a regression that explains the score of students in the final exam of a course in statistics in terms of the score in a previous home assignment, yields an intercept  $b_0 = -25.2$  and a slope  $b_1 = 1.5$ . The predicted score in the final exam for a student with 50 points in the home assignment is:
  - (a) -1258.5;
  - (b) -1185.0;
  - (c) 12.2;
  - (d) 49.8;
  - (e) 75.0.
- 12. Two teachers, Teacher 1 and Teacher 2, are in charge of grading 100 exams of statistics. 50 exams are randomly assigned to teacher 1 and the remaining 50 are assigned to teacher 2. The following table summarizes the results:

	Grade						
Teacher	A	В	С	D	Ε	Fx	F
1	2	2	6	12	8	4	16
2	2	6	7	8	7	4	16

Having a significance level  $\alpha = 0.05$ , what is the critical value for the hypothesis that grade and teacher are independent:

- (a) 2.944;
- (b) 12.592;
- (c) 17.000;
- (d) 67.505;
- (e) none of the above.

#### Part two. Complete solution

13. A Formula 1 team is considering to implement a new setup on its cars which will significantly improve the lap times. However, there is concern about the effect that this setup may have on the life of the tyres (i.e. the number of laps before the tyres need to be changed). Thus, the team will test the new setup and measure the life of the tyres.

By experience, the team knows that the life of the tyres can be adequately described by a normal distribution with a standard deviation of 2.5 laps.

- (a) What is the smallest sample size needed if they want to estimate the life of the tyres through a 95% confidence interval with a length no larger than one. (**Note**: the length of a confidence interval is the difference between the upper and the lower limits) (5p.)
- (b) The team decided to test 100 sets of tyres and measure its life. The results are summarized in the following table.

Find the sample mean of the tyre's life,  $\bar{x}_s$ . (5p.)

- (c) Find a 95% confidence interval for the life of the tyres. (**Note**: If you did not solve 13b use  $\bar{x}_s = 11$ .) (5p.)
- (d) Based on historical records, it is known that the tyre's life expectation with the previous setup is equal to 12 laps. Using a significance level of 5%, test the hypothesis that the new setup has had any effect on the tyre's life (i.e. test the two-sided alternative). (**Note**: If you did not solve 13b use  $\bar{x}_s = 11$ .) (5p.)
- 14. A machine produces, at random, pyramids and cubes of three different colors (black, white or red).
  - (a) The machine's operator sets the probability with which the machine will produce each combination of shape and color. During one particular day, the operator has set the following probabilities:

		Color		
		Black	White	Red
	Pyramid	0.2	0.25	0.1
Shape	Cube	0.0	0.05	0.4

Are the shape and the color independent of each other? (5p.)

(b) A customer (who does not know the probabilities set by the operator) wants to determine if the machine is producing objects whose shape and color are chosen independently. To this end, he asks the operator to activate the machine n=10 times. The results are summarized below:

		Color			
		Black	White	Red	
	Pyramid	1	1	1	
Shape	Cube	0	1	6	

Using a significance level of 5%, test if the machine is producing objects whose shape and color are chosen independently. (5p.)

(c) A second customer (who does not know the probabilities set by the operator either) also wants to determine if the machine is producing objects whose shape and color are chosen independently. To this end, she asks the operator to activate the machine n = 100 times. The results are summarized below:

		Color			
		Black	White	Red	
	Pyramid	17	21	10	
Shape	Cube	0	4	48	

Using a significance level of 5%, test if the machine is producing objects whose shape and color are chosen independently. (5p.)

(d) What are your conclusions on the results in 14a, 14b and 14c? (**Hint:** Take into account that from 14a you know if the hypothesis holds or not.) (5p.)